

CYPHERING/DECYPHERING PERFORMED BY AN INTEGRATED CIRCUIT

BACKGROUND OF THE INVENTION

Field of the Invention

The present invention relates to the cyphering of digital data by means of algorithms intended to mask original data to make them undetectable by a possible pirate. The present invention more specifically relates to algorithms implementing a same transformation on different parts of the data to be coded.

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Discussion of the Related Art

The cyphering/decyphering algorithms to which the present invention applies are generally executed by integrated circuit, either by means of state machines in wired logic, or by means of microprocessors executing a program in memory (generally a ROM).

15 Such algorithms use secret keys specific to integrated circuits or to the user, which are exploited by the algorithm to code the data.

An example of a cyphering/decyphering algorithm to which the present invention most particularly applies is an algorithm known as the AES (Advanced Encryption Standard, FIPS PUB 197). This algorithm applies to a word or data code divided into
20 blocks a same transformation several consecutive times based on different cyphering keys or, more specifically, on portions of a binary word forming a key.

Fig. 1 illustrates in a simplified flowchart the main steps of a conventional AES-type algorithm. Only the cyphering will be described, the decyphering using the inverse transformations.

25 This algorithm cyphers a word or code S_0 of a predetermined number of bits (generally, 128 bits) into another word or code S_n of same size. The data to be cyphered are in fact formed of several words or codes resulting from a previous division of the data into words all having the same size. The cyphering and the decyphering are based on a secret key, the length of which (generally from 128 to 256 bits) conditions the cyphering
30 security.

In practice, each step of an AES-type algorithm processes a matrix of four lines and four columns representing a word and each element of which is a byte or block of the processed 128-bit code. To simplify the following description, reference will be made

for each step to a state considered as being a matrix.

To implement the cyphering or decyphering algorithm, 11 sub-keys each also comprised of 128 bits are first generated based on the secret key over 128 bits. More generally, based on a secret key of a number m of bits, $n+1$ sub-keys $K_0, \dots, K_i, \dots, K_n$ of m bits each are derived. These sub-keys are intended to be used by the algorithm as will be described hereafter in relation with Fig. 1.

The algorithm starts from an initial state (block 1, STATE INIT) S_0 of the code or data word to be cyphered.

A first phase of the cyphering process is a so-called “bleaching” operation (block 2, ADDROUNDKEY) which consists of performing an XOR-type combination of initial state S_0 with first sub-key K_0 . A first intermediary state S_1 is obtained.

A second phase of the cyphering process consists of performing several turns or cycles of a same transformation T involving, at each turn, the state S_{i-1} obtained at the preceding turn and a current sub-key K_i . The number of turns of transformation T corresponds to $n-1$, that is, to the number of derived sub-keys, minus 2.

Each turn of transformation T is formed of four successively-applied operations. Fig. 2 illustrates in more detail these four operations on a matrix 20 of four lines and four columns of binary bytes to which an AES-type algorithm applies.

A first step (block 3, SHIFROWS) consists of performing a rotation on the last three lines of matrix 20. First line 201 of matrix 20 is left unchanged. Second line 202 is rotated by one byte. Third line 203 is rotated by two bytes. Fourth line 204 is rotated by three bytes.

A second step (block 4, SUBBYTES) of a turn of transformation T is a non-linear transformation in which each byte of matrix 20' forming the current state is replaced with its image taken from a substitution box (SBOX). As illustrated in Fig. 2, substitution box SBOX is obtained by two successive transformations. A first transformation (block 41, INV) consists of inverting the considered byte (the element of matrix 20') in the finite body of order 2^8 (to correspond to the byte), byte 00 forming its own image. This inversion is followed by an affine transformation (block 42, AFFINE).

Examples of non-linear substitution transformations such as that disclosed hereabove are described, for example, in work “The Design of Rijndael” by Joan Daemen and Vincent Rijmen, published by Springer-Verlag (ISBN 3-540-42580-2) and

in the AES standard (FIPS PUB 197).

The third step (block 5, MIXCOLUMNS) of the turn of transformation T consists of considering each column of matrix $20''$ resulting from the preceding step as a polynomial on the finite body of order 2^8 , and of multiplying each of these polynomials by a combination polynomial $P[X]$ modulo a polynomial $M[X]$.

The last and fourth step of the turn of transformation T of rank i consists of applying sub-key K_i to matrix $20''$ of the previous state to obtain a matrix $20'''$, in which each element of matrix $20''$ has been combined by XOR, bit to bit, with sub-key K_i (block 6, ADDROUNDKEY). Step 6 is the same as step 2 of the first cyphering phase, but performed with a different sub-key.

At the end of step 6, one obtains, for a turn of rank i, a state $S_i = T(K_i, S_{i-1})$. The four steps of the turn transformation are repeated n-1 times, that is, after step 6, it is returned to step 3 to perform a new turn with a next key.

The third phase of the cyphering algorithm (Fig. 1) consists, in a way, in a last turn, slightly modified as compared to that illustrated in Fig. 2. In fact, the steps of the turn transformation are reproduced except for the third one (MIXCOLUMNS). This amounts to successively performing steps 7, 8, and 9 corresponding to previously-described steps 3, 4, and 6 with, as the key for step 9, the last sub-key K_n .

State $S_n = T'(K_n, S_{n-1})$ is then obtained. This result is finally set up (block 10, RESULTFORM) for a subsequent use.

A known weakness of implementations on smart cards of AES-type algorithms or more generally of algorithms implementing several turns or cycles of a same transformation (T) on a code divided into blocks, is the sensitivity to attacks by analysis of the current consumption of the circuit executing the algorithm. Such an attack known as a DPA (Differential Power Analysis) consists of correlating the consumption of the integrated circuit executing the algorithm with the secret keys used upon cyphering or decyphering. In practice, based on a message to be cyphered and on hypotheses about the secret key, a statistic correlation curve is established along time between the consumption of the product for the message cyphering and an intermediary value calculated by the circuit. Such consumption attacks are described in literature (see, for example, article "Differential Power Analysis" by Paul Kocher, Joshua Jaffe, and Benjamin Jun, published in 1999, CRYPTO Conference 99, pages 388-397, published by

Springer-Verlag LNCS 1666).

A known solution to make the algorithms more resistant against differential power analysis attacks of the integrated circuit, consists of involving a random number in the execution of the algorithm. The use of a random value consists of masking the state at the beginning of the algorithm by this random value and of restoring the expected result at the end of the algorithm.

Fig. 3 partially and very schematically illustrates a first known technique of introduction of a random number R_d in the execution of an AES-type algorithm. Starting from an initial state of the matrix (block 11, STATEINIT), a bit-to-bit XOR type combination (block 12, +) with a random number R_d is performed. This number is thus introduced before step 2 of combination with first sub-key K_0 . This random number R_d must then be taken into account at some stages of the algorithm. First, in non-linear transformation steps 4 and 8 (SUBBYTES), a substitution box ($SBOX_{R_d}$) taking the random number into account must be used. Then, for each turn transformation, after the introduction of current key K_i (step 6), an XOR-type combination (block 13, +) with number R_d must be performed. Moreover, after step 13, the obtained result is combined (block 15, +) by XOR with an amount $MC(SR(R_d))$ corresponding to the application of the row shifting SR (SHIFTROWS) and column mixing MC (MIXCOLUMNS) functions to number R_d .

After the last transformation T' , the combination (block 16, +) by XOR of the obtained result with value $SR(R_d)$ corresponding to the application of the row shifting to value R_d enables recovering the expected result.

The necessary use of a substitution box which is a function of the random number compels to recalculate this box for each cyphering or decyphering. This recalculation of the substitution boxes, necessary to obtain a good resistance against DPA attacks, results in a strong need for memory in the integrated circuit and lengthens the algorithm execution time by the necessary calculation time. For example, for codes (matrixes) over 128 bits, the recalculation of a substitution box $SBOX_{R_d}$ for each byte of the state requires 16 boxes of 256 bytes, which amounts to 4 kilobytes of memory. Such a memory is far from being negligible when integrated, for example, in a smart card.

Fig. 4 illustrates a second conventional solution to involve a random value in a cyphering algorithm of AES type. This solution is described in article "An

implementation of DES and AES, secure against some attacks” by M.L. Akkar and C. Giraud, published at the CHES conference 2001 (Springer-Verlag editors).

This solution consists of replacing the use of substitution boxes with transformations calculated at each turn of the algorithm. The result is the same, in that it
5 leads to a substitution of the different matrix bytes. What changes is the way to obtain this substitution.

According to this solution, two random numbers Rd1 and Rd2 are used, and made to intervene at different steps of the algorithm. First random number Rd1 intervenes at the beginning (between blocks 1 and 2) and is added (XOR-type
10 combination 22). Second random value Rd2 is introduced into the turns of the transformation, be it the $n-1$ identical transformations T or the last transformation T’.

The result of row shifting step 3 or 7 is combined by a polynomial multiplication
23 with coefficients on the finite body of order 2^8 (modulo an irreducible polynomial) with random value Rd2. Then, the obtained resulting matrix is added (XOR-type
15 combination) with a matrix representing the result of the previous operation ($S_i * Rd2$). This addition is symbolized by a block 25 in Fig. 4.

The two previous operations are performed before byte substitution step 24 which here is essentially comprised of two transformations. A first transformation (block 241, INV) consists of inverting each byte of the matrix resulting from step 25. Then, the
20 product (byte by byte modulo an irreducible polynomial) of initial state S_i by the inverse ($Rd2^{-1}$) of the random value is added (XOR) to this inverse matrix (block 242, +). The result is then multiplied (block 243, X) by random value Rd2. There again, this is a polynomial multiplication. Finally, the last byte substitution step 24 of the matrix consists in an affine transformation 244 (AFFINE). At the end of step 24, the resulting
25 matrix is submitted to the step of addition of the corresponding sub-key (step 6 or 9).

In a turn of a transformation, the step following step 24 is step 5 (MIXCOLUMNS). Then, after step 6, the obtained result is combined (block 26, +) by XOR with value Rd1. The result of addition 26 is combined (block 27), still by XOR, with result ($MC(AF(SR(Rd1)))$) of the polynomial column mixing processing (MC) of
30 affine transformation AF applied to the row shifting SR applied to value Rd1.

In last transformation T’, the step following step 24 is step 9 with key K_n . Finally, the obtained result is combined (block 29, +) by XOR with the result

(AF(SR(Rd1))) of affine transformation AF applied to row shifting SR applied to value Rd1. The output of block 29 provides the state to be set up by step 10.

Such a solution requires less memory than the first conventional solution illustrated in relation with Fig. 3. However, it considerably increases the algorithm execution time. Indeed, at each turn of the algorithm, the operation corresponding to the substitution becomes complex and requires many operations modulo a polynomial.

The problem of the processing by a random number is essentially due to the fact that, in an algorithm of the type to which the present invention applies, the substitution operation is a non-linear operation.

Summary of the invention

The present invention aims at providing a novel solution to the introduction of at least one random value in an AES-type cyphering algorithm which overcomes the disadvantages of known solutions. More generally, the present invention aims at providing the introduction of at least one random value in an algorithm submitting a code or input word, divided into blocks, several times to the same transformation (by a substitution matrix) with different keys.

The present invention also aims at providing a solution which minimizes the number of times that a substitution box must be calculated and/or stored.

The present invention also aims at minimizing the calculation time necessary to the execution of the algorithm after introduction of the random number.

To achieve these and other objects, the present invention provides a cyphering/decyphering method, by an integrated circuit, of a digital input code by means of several keys, consisting of:

- dividing said code into several data blocks of same dimensions; and
- applying to said blocks several turns of a cyphering or decyphering consisting of submitting each block to at least one same non-linear transformation and of subsequently combining each block with a different key at each turn,
- the operands being masked, upon execution of the method, by means of at least one first random number having the value of said code and all the blocks of which have the same size by combining, by an XOR-type function, the input and output blocks of the non-linear transformation with said random number.

According to an embodiment of the present invention, the input code is combined with a second random number of same dimension as the code.

According to an embodiment of the present invention, said non-linear transformation consists of using a box of substitution of the input code blocks, calculated
5 with a third random number of same length as said code and all the blocks of which have the same value. According to the present invention, said box respects the fact that the transformation of an input code, previously combined by XOR with the first random number, corresponds to the result of the combination by XOR of this input code with said third random number.

10 According to an embodiment of the present invention, the method is applied to an AES-type cyphering algorithm.

According to an embodiment of the present invention, said first random number is changed at each cyphering turn.

According to an embodiment of the present invention, said second random
15 number is changed at each cyphering of new data.

According to an embodiment of the present invention, said third random number is changed at each cyphering turn.

The present invention also provides an integrated circuit comprising a block for cyphering/decyphering by turn input data divided into blocks of same dimensions,
20 comprising:

means for generating at least one first random number of same size as the size of the blocks of the input data; and

means for combining said random number with each block, at the input and at the output of a non-linear transformation implemented by the cyphering/decyphering.

25 The foregoing objects, features and advantages of the present invention, will be discussed in detail in the following non-limiting description of specific embodiments in connection with the accompanying drawings.

Brief Description of the Drawings

30 Fig. 1, previously described, illustrates in a simplified flowchart a conventional cyphering method of the type to which the present invention applies;

Fig. 2, previously described, illustrates the processings performed on a matrix

state in a turn of a transformation of the method of Fig. 1;

Fig. 3, previously described, shows the steps of a first conventional method of taking into account of a random number in a cyphering algorithm of the type illustrated in Fig. 1;

5 Fig. 4, previously described, shows a second conventional solution of introduction of random numbers in a cyphering algorithm of the type shown in Fig. 1;

Fig. 5 illustrates in a simplified flowchart an embodiment of a cyphering algorithm according to the present invention; and

10 Fig. 6 shows, in a simplified flowchart, an embodiment of a decyphering method according to the present invention.

Detailed Description

For clarity, only those steps that are necessary to the understanding of the present invention have been shown in the drawings and will be described hereafter. In particular, the processings upstream and downstream of the cyphering algorithm have not been detailed and are no object of the present invention. Further, the operations of division of the secret quantity into several sub-keys to be taken into account by the algorithm, as well as the generation of the adapted random numbers have not been detailed and are within the abilities of those skilled in the art based on the indications which will be given hereafter.

20 According to the present invention, a random value having the same size as the state to be cyphered (the matrix) is used for the transformations processing several bytes at the same time or which mix them together, as is the case for transformations of column mixing, sub-key introduction, and row shifting type.

25 However, this random value is not used for non-linear functions, such as those implemented for the byte substitution by a substitution box in the considered case. According to the present invention, a substitution box is masked by another random value, the bytes of which (or more generally, the blocks of a size corresponding to the size of the blocks of the code taken into account in the substitution box) are all identical. 30 Although it is thus performed by means of a random value of one byte, such a masking operation is efficient since, due to the complete masking of the functions operating over the entire block, it is not possible for a pirate to exploit this specificity through a

correlation function. According to an alternative embodiment, a pseudo-random value, linked to this random value, is also used to mask the substitution box.

Fig. 5 shows a flowchart of an implementation mode of an AES-type algorithm, masked by means of random and/or pseudo-random values according to the present invention.

In the following description, reference will be made to the sizes of binary words, taking the example of an AES algorithm using a 128-bit key and a division of a 128-bit input code in the form of an array of four rows and four columns of bytes. It should however be noted that all that will be described hereafter applies whatever the size of the keys and of the input and output codes, provided that the possible relations therebetween be respected. In particular, it should be noted that the size of the random values (possibly the pseudo-random values) used for the substitution box must correspond to the size of a matrix element, while the size of the random value (possibly, the pseudo-random value) used for the linear transformations must correspond to the size of a complete input state. By definition, an XOR-type combination is designated as the addition, a polynomial multiplication modulo an irreducible polynomial is designated as the multiplication.

In the left-hand portion of Fig. 5, the successive steps of the cyphering algorithm have been shown, while in the right-hand portion of this drawing the states obtained at the end of each step have been indicated.

The process starts from an initial state (block 31, STATE INIT). State S_0 corresponds to the code (data) to be cyphered by the algorithm.

First step 41 consists of performing an XOR-type combination of state S_0 with a random value R having the same size as state S_0 (for example, 128 bits).

Then, a conventional step 32 of sub-key addition (block 32, ADDROUNDKEY) by an XOR-type combination of first sub-key K_0 with the result of the preceding step is executed. The obtained state corresponds to state S_1+R .

The second phase of the cyphering method consisting of executing $n-1$ turns of a same transformation T is then entered. This transformation involves the steps of the conventional process (for example, AES) which are desired to be masked by at least one random value. In the example shown, these are row shifting step 33 (SHIFTRROWS), step 34 (SUBBYTES) of byte substitution by means of a substitution box SBOX, column mixing step 35 (MIXCOLUMNS), and step 36 of XOR combination

(ADDDROUNDKEY) with sub-key K_i of rank i .

According to the present invention, between these steps, two random values R_1 and R_2 (possibly, $R_1=R_2$) each formed of sequences of bytes of same value are introduced. The number (for example, 16) of bytes of each value corresponds to the
5 number of bytes of a processed state (for example, 128 bits).

At the output of step 33, a matrix having shifted rows from state matrix S_i combined with random value R is obtained. Designating the row shifting function as SR , the following can be written at the end of step 33: $SR(S_i+R)=SR(S_i)+SR(R)$.

According to the present invention, before performing the substitution of step 34,
10 state $SR(S_i)+SR$ is combined (block 42) with a value of same size ($R_1+SR(R)$) corresponding to the application of the row shifting to random value R ($SR(R)$) combined, byte by byte, by XOR with random value R_1 . In other words, the state is masked by a value of same size, each byte of which has the same random value.

Step 34 of byte-by-byte substitution by means of substitution box $SBOX_{R_1,R_2}$ is
15 then performed. This box is, according to the present invention, a function of value R_2 and is linked to value R_1 , respecting the following relation:

$SB(S_i+R_1)=SBOX(S_i)+R_2$, where $SBOX$ represents the substitution box of the algorithm that is desired to be masked and SB designates the byte substitution function (SUBBYTES). In other words, a new substitution box SB is calculated based on table
20 $SBOX$ of the algorithm which is desired to be masked by values R_1 and R_2 .

To the result ($SB(SR(S_i))+R_2$) of step 34 which corresponds to a state masked by value R_2 (each byte of the matrix is masked by a byte of same value), an XOR-type combination is applied (block 43) with XOR combination R_2+R (byte by byte) of the value R over 128 bits and of byte R_2 .

25 The result ($SB(SR(S_i))+R$) undergoes column mixing transformation 35 of the conventional algorithm. Still respecting the conventional algorithm, sub-key K_i is introduced by step 36 of XOR combination with the preceding matrix. Result $MC(SB(SR(S_i)))+MC(R)+K_i$, where MC designates column mixing function MIXCOLUMNS, is combined (block 44) with a matrix corresponding to the sum (XOR-type combination) of random value R and of this same value $MC(R)$ having undergone a
30 column mixing transformation identical to transformation 35.

The cyclic transformation ends with step 44 at the end of which, according to

rank i , it is returned to step 33 for a new iteration, or it is proceeded to step row shifting 37 (SHIFROWS) of the last transformation T .

There again, the present invention consists of interposing, between some steps of the algorithm, the execution of which is desired to be masked by random values, logic combinations of the matrixes processed by values $R1$ and $R2$.

The transformation by substitution matrix 38 is identical to that described in relation with step 34, but framed by combinations 45 and 46. These combinations are identical to previously-described combinations 42 and 43, upstream and downstream of transformation 34.

At the end of step 46, the obtained matrix $SB(SR(S_{n-1}))+R$ is combined with the last sub-key K_n (block 39). Then, the expected result is restored $(SB(SR(S_{n-1}))+K_n)=T^{-1}(S_{n-1}, K_n)$ by recombining (block 47, +) by XOR the matrix obtained with first random value R of same size as this matrix. Result S_n is then conventionally set up (block 40, RESULTFORM).

An advantage of the present invention is that quantities $R1$ and $R2$ as well as substitution box SBOX can be recalculated at each turn T of the cyclic transformation or at each cyphering or decyphering of the input data by the complete algorithm.

Another advantage of the present invention is that a memory corresponding to twice the matrix to be processed is sufficient to store the new substitution boxes (the old one and the new one) since said matrixes are combined with a random value, the size of which corresponds to that of an element of the matrix.

Fig. 6 shows, in the form of a simplified flowchart, an embodiment of an algorithm for decyphering data S_n according to the present invention.

As in the algorithm, the execution of which is desired to be masked by random values, the decyphering resumes the steps inverse of those of the cyphering except for the step of introduction of the keys or sub-keys K_i , which are performed in the reverse order.

The initial state (block 51, STATE INIT) here corresponds to a cyphered or encrypted state (S_n) of the data.

As for the cyphering algorithm, the initial state is first combined (block 61) with a random quantity R having the same size as the initial data. Then, the obtained state S_n+R is combined (block 52, ADDROUNDKEY) with the sub-key K_n which corresponds to the last portion of the cyphering key (in this example, the last byte). The obtained state

$S_{n-1}+R$ is then submitted to $n-1$ cycles of a same decyphering transformation taking into account at each turn a sub-key K_i of lower rank.

The successive steps can be deduced from the previously-described cyphering steps:

- 5 - shifting of inverse rows (block 53, INVSHIFROWS, function ISR) corresponding to the inverse transformation of that of block 33;
- XOR-type combination 62 with random quantity R_1 and function 53 applied to random quantity R (ISR(R));
- application (block 54, INVSUBBYTES, function ISB) of the inverse
10 substitution box $INVSBOX_{R_1, R_2}$ of that used at step 34;
- XOR-type combination 63 with quantities R_2 and R ;
- inverse transformation (block 55, INVMIXCOLUMNS, function IMC) of the so-called column mixing transformation 35;
- XOR-type combination (block 56, ADDROUNDKEY) with the sub-key K_i of
15 rank i ; and
- XOR-type combination 64 with random quantity R and with the result of a transformation 55 (IMC) applied to this random quantity.
- steps 62, 63, and 64 are identical to steps 42, 43, and 44 executed on cyphering. Steps 52, 53, 54, 55, and 56 correspond to the functions conventionally implemented for
20 the decyphering of the algorithm, the execution of which is desired to be masked.

At the end of the last turn of this cyclic transformation, steps 57, 58, and 59 inverse of cyphering steps 37, 38, and 39 and corresponding to the conventional steps of the decyphering method, are successively applied, interposing the same combination steps 65, 66, and 67 as upon cyphering.

- 25 The result matrix S_0 corresponding to the decyphered data is thus obtained.

Of course, the present invention is likely to have various alterations, modifications, and improvement which will readily occur to those skilled in the art. In particular, the present invention which has been described hereabove in relation with the AES-type cyphering algorithm may be transposed to any cyphering algorithm, the input
30 code of which is divided into blocks of identical sizes to be ciphered, each block being submitted to a same non-linear transformation.

Further, the adaptation of the present invention and of the sizes of the random

quantities and of the used keys is within the abilities of those skilled in the art. It will be ascertained to respect a number of sub-keys corresponding to the numbers of turns and a size of random quantity R corresponding to the size of the sub-keys, and thus of the blocks. Moreover, the numbers indicated as being random numbers may originate from a
5 pseudo-random generator.

Finally, the present invention applies whatever the use made of the ciphered data.

A specific example of application of the present invention relates to the implementation of an AES-type cyphering/decyphering algorithm in a smart card.

Such alterations, modifications, and improvements are intended to be part of this
10 disclosure, and are intended to be within the spirit and the scope of the present invention. Accordingly, the foregoing description is by way of example only and is not intended to be limiting. The present invention is limited only as defined in the following claims and the equivalents thereto.

What is claimed is: